# УДК (UDC) 656.025.4:656.073.7 <br> ВЛИЯНИЕ ВРЕМЕНИ ОЖИДАНИЯ В ОЧЕРЕДИ НА ВРЕМЯ ДОСТАВКИ <br> THE EFFECT OF QUEUE ON DELIVERY TIME 

Чандра А. ${ }^{1}$, Наталиа К. ${ }^{2}$<br>Agung Chandra ${ }^{1}$, Christine Natalia ${ }^{2}$<br>${ }^{1}$ - Университет Мерку Буана (Джакарта, Индонезия)<br>${ }^{2}$ - Католический университет Индонезии Атма Джая (Джакарта, Индонезия)<br>${ }^{1}$ - Universitas Mercu Buana (Jakarta, Indonesia)<br>${ }^{2}$ - Universitas Katolik Indonesia Atma Jaya (Jakarta, Indonesia)

Аннотация. Планирование марирута - сложная проблема в сфере перевозок и поэтому необходимо учитывать несколько факторов, начиная с вместимости транспортного средства и потребительского спроса, распределения водителей для перевозки, расстояния, времени в пути. Транспортировка, как один из ключевых элементов логистики и две трети логистических затрат, нуждается в дальнейшем изучении. В этой статье изучалось влияние ожидания в очереди на время в пути, которое могло произойти в магазине покупателя. В этом исследовании были собраны соответствующие данныее которые включали три грузовика, двадцать четыре координаты покупателей-детских магазинов, вместимость грузовиков и объем товаров. Связанными теориями были задача множественного коммивояжера и теория массового обслуживания - один сервер и использование дисциплины FIFO - первый вход, первый выход (M/M/1), а также экспонениииально распределенная случайная величина. Маршрут начался с главного склада в 08:30 из Тангеранга, заказы были отправлены клиентам, расположенным в Джакарте, обеденный перерыв с 12:00 до 13:00 и возвращение на главный склад до 17:30 с обычной скоростью. OptimoRoute, как одно из подходящих программ для решения проблемы маршрутизации транспортных средств, использовалась для определения последовательности отправки, распределения заказов для водителей и необходимого времени. Онлайн-симулятор использовался для устранения эффекта очереди. Результаты показали, что время в пути на каждую остановку увеличивалось примерно на пятнадйать минут; чем больше магазинов, тем больше времени требовалось. Это дополнительное время может повлиять на стоимость сверхурочных, если время в пути превышает рабочие время. Планировщик должен учитыьать время ожидания в очереди при планировании следующего марирута.
Ключевые слова: планирование маршрута, ожидание в очереди, время в пути.

Дата получения статьи:
21.07.2023

Дата принятия к публикации:
15.08.2023

Дата публикации.


#### Abstract

Route planning is a complex problem in transportation, and one has to consider several factors starting from vehicle's capacity and customer's demand, allocation of drivers for shipment, distance, travel time. Transportation as a one of the key elements in logistics and two third logistics costs, needs study further. This paper studied the effect of queuing activity on travel time that could be happened at customer's shop. This study collected the related data which were three trucks, twenty-four coordinates of customers-baby shops, capacities of trucks, and volume of goods. The related theories were multiple traveling salesman problem (mTSP) and queuing theory - single server and using the FIFO - First In First Out discipline (M/M/1), and exponential distributed random variable. The route started from the main warehouse at 08:30 from Tangerang, shipped the orders to the customers located in Jakarta,, lunch break 12:00 to 13:00 and return to the main warehouse before 17:30 by using normal speed. OptimoRoute as one of the suitable software for solving the vehicle routing problem was used to solve the sequence of shipment, order allocation for drivers and time needed; where On Line Simulator was used to solve the effect of queue. The results indicated that there was an additional time around fifteen minutes per stop to travel time; the more shops, the longer time was needed. This additional time may impact the overtime cost if the amount of travel time exceeds the working hour and queuing time must be considered for the next route planning by the planner.


Keywords: route planning, queuing activity, travel time.

| Date of manuscript reception: | 21.07 .2023 |
| :--- | :--- |
| Date of acceptance for publication: | 15.08 .2023 |
| Date of publication: | 25.09 .2023 |

21.07.2023
25.09.2023

## Сведения об авторах:

Чандра Агунг - магистр гражданского строительства и финансового менеджмента, старший преподаватель кафедры промышленного инжиниринга Университета Мерку Буана, email: agung.chandra@mercubuana.ac.id.

ORCID: https://orcid.org/0000-0002-0338-1588
Наталиа Кристина - магистр промышленного инжиниринга, старший преподаватель кафедры промышленного инжиниринга Католического университета Индонезии Атма Джая, e-mail: chrisnatalia@atmajaya.ac.id.

ORCID: https://orcid.org/0000-0002-4260-684X

## Authors' information:

Agung Chandra - Master in Civil Engineering and Financial Management, Senior Lecturer, Department of Industrial Engineering, Universitas Mercu Buana, email: agung.chandra@mercubuana.ac.id.

ORCID: https://orcid.org/0000-0002-0338-1588
Christine Natalia - Master in Industrial Engineering, Senior Lecturer, Department of Industrial Engineering, Universitas Katolik Indonesia Atma Jaya, e-mail. chrisnatalia@atmajaya.ac.id.

ORCID: https://orcid.org/0000-0002-4260-684X

## Благодарности

Исследование было поддержано и профинансировано Университетом Мерку Буана и Католическим Университетом Индонезии Атма Джая (проект № 02-5/863/B-SPK/V/2023)

Acknowledgements<br>The study was supported and funded by Universitas Mercu Buana and Universitas Katolik Indonesia Atma Jaya (project No. 02-5/863/B-SPK/V/2023)

## 1. Introduction

It is essential to offer products and services to consumers at the desired time and place and to deliver them on time [1]. When delivering goods or services, time becomes a critical issue for driver, in this paper we call time as a travel time. The sensitivity to travel time is usually referred to value of time. There are some factors that affect travel time, such as length or distance, congestion such as parking of vehicles along the route, delay such as number of stops, number of signalized inter-section, accident, and environment such as route direction [2,3]. Distance relates to velocity and time, when distance become farther then time needed to travel become longer. Congestion is a condition that arises because more people wish to travel at a given time than the transportation system can accommodate: a simple case of demand exceeding supply [4] and congestion makes vehicle run slower and take more time than normal to arrive at customer's destination and congestion can be avoided by choosing another route. The route choice problem can be stated as follows. Given a transportation network composed of nodes, links, origins and destinations; and given an origin, a destination and a transportation mode, what is the chosen route between origin and destination on mode [5]. Transportation is a key element of logistics, and it occupies around one third to two third of logistics cost [6], then it is
important to minimize the cost of transport. Delay also affects delivery time, and queue happens when many trucks are waiting for unloaded by customer. This waiting line depends on number of trucks and goods that are ready to be unloaded. Trucks that wait for unloaded cannot be predicted by driver, and this queue makes travel time longer than normal. When supplier's driver delivers goods to customer or baby shop, he often finds that he is not the only supplier who delivers goods at the time, then, he has to wait in line until all suppliers that come before him have been finished. From this reality, planning route should consider not only travel time from starting point to destination's point, but also the amount of time that spent in a customer's place especially queue.

In this paper, the objective of research is to know how big the effect of queue for unloading process on travel time from Tangerang to Jakarta - capital city during office hours. This result will help transportation planner allocating the right amount of customer's point to driver.

## 2. Methods and materials

### 2.1. Multiple Traveling Salesman Problem

The multiple traveling salesman problem (mTSP) is a generalization of the well-known traveling salesman problem (TSP), where more
than one salesman is allowed to be used in the solution [7]. The characteristics of the mTSP seem more appropriate for real-life applications, such as robotics, transportation and delivery, networking, disaster management, precision agriculture, search and rescue [8], order picking [9]. Mathematical model for mTSP is as follows:

The m-TSP is defined on a graph $G=(V, A)$, where $V$ is the set of vertices or nodes and $A$ is the set of arcs or edges. Let $C=\left(c_{i j}\right)$ be the cost or distance matrix defined on the set of $A$. The matrix $C$ is said to be symmetric when $\left(c_{i j}\right)=\left(c_{j i}\right)$, $\forall(i, j) \in A$ and otherwise is said to be asymmetric. If the cost matrix satisfies $c_{i j} \leq c_{i k}+c_{k j}$ for $\forall_{i, j, k}$ then the matrix $C$ satisfies the triangle inequality. There are various models have been proposed for the m-TSP in the literature, but assignment based mathematical model, tree based mathematical model and a three-index flow-based model have been widely used. The three-index flow-based model for the m-TSP is as follows:

Let $n$ be the number of cities or pick locations, and $m$ be the number of salesmen or pickers (we assume $n \geq 3 m+1$ ), then the variable $x_{i j}$ is defined as follows [10]:

$$
x_{i j}=\left\{\begin{array}{c}
1, \text { if edge }(\mathrm{i}, \mathrm{j}) \text { is used in the tour } \\
0, \text { otherwise }
\end{array}\right.
$$

Goal Function: Minimize:

$$
\begin{equation*}
\sum_{(i, j) \in A} c_{i j} x_{i j} \tag{1}
\end{equation*}
$$

Constraints:

$$
\begin{align*}
& \sum_{\substack{j=2 \\
n}} x_{1 j}=m  \tag{2}\\
& \sum_{j=2}^{n} x_{j 1}=m  \tag{3}\\
& \sum_{\substack{i=1 \\
n}} x_{i j}=1, j=2, \ldots n  \tag{4}\\
& \sum_{j=1}^{n} x_{i j}=1, j=2, \ldots n  \tag{5}\\
& \sum_{i \in S} \sum_{j \in S} x_{i j} \leq|S|-1, \forall S \subseteq V-1, S \neq 0  \tag{6}\\
& x_{i j}=0 \vee 1,(i, j) \in A
\end{align*}
$$

In this research, there were 3 trucks that shipped goods everyday from warehouse where
located in Jatiuwung, Tangerang to 24 baby shops then returned to warehouse.

### 2.2. Waiting Line - Queue

Waiting line is also called queue and is where customers wait before being served [11] and become part of our daily activities such as paying for goods in department store, buying a movie ticket, ordering food in a restaurant, emergency room at the hospital and so on. Waiting causes inefficiency, for example when delaying service jobs exceeded their due dates may result in lost future business, waiting for unloading goods, administration and checking process from truck to floor may disrupt delivery for next customer. Queues arise when the shortterm demand exceeds the capacity.

The components of queuing systems are arrival process, service and departure process, queuing discipline, system capacity, number of servers, and population size [12]. In this research, service discipline is FIFO because unloading process is based on which vehicle comes first and only one server at the baby shop, then when server serves and checks the goods for one supplier, he cannot serve another supplier.

Common used formulas are as follows:

$$
\begin{align*}
& L=\lambda W  \tag{8}\\
& L_{q}=\lambda W_{q}  \tag{9}\\
& W=W_{q}+\frac{1}{\mu}  \tag{10}\\
& L=\lambda\left(W_{q}+\frac{1}{\mu}\right)  \tag{11}\\
& \rho=\frac{\lambda}{\mu} \tag{12}
\end{align*}
$$

where $L$ - expected number of customers in the system, including those being served; $L_{q}$ - expected number of customers in the queue; $W$ expected waiting time in the system, including service time for individual customer; $W_{q}$ - expected waiting time in the queue; $\lambda$ - mean arrival rate for customers coming to the queueing systems or expected number of arrivals per unit time; $\mu$ mean service rate or expected number of service completions per unit time; $1 / \lambda$ - expected interarrival time or the average time be-
tween the arrival of consecutive customers; $1 / \mu$ - expected service time for each customer.

### 2.3. Transportation and Queuing Software

### 2.3.1. Transportation software

In this research, OptimoRoute software was used to solve the multiple traveling salesman problem. OptimoRoute was regarded as one of the suitable software for solving vehicle routing problem and had following advantages: high ease of use, the clarity with which solutions are shown, both graphically and analytically, through the use of colors and the sense of the streets, and the high amount of data from the different routes illustrated in the solutions. There were also some disadvantages: free-30 day-trial, if the destination points are very close to each other, the graphical interpretation becomes confusing [13]. OptimoRoute is a routing optimization software, created in 2012 in the United States, used by multiple companies from different business sectors around the world. The program was at www.optimoroute.com [14].

### 2.3.2. Queuing software

Queuing on-line simulator was used to calculate the results of research data. This simulator was created by Associate Professor Jaroslav Sklenar, Department of Statistics and Operations Research, University of Malta and its software can be found at www.staff. um.edu.mt/jskl1/simweb/simdown.html [15].

### 2.4. Methods

The study was conducted at textile company which its warehouse located in Tangerang and categorized as a small and medium enterprise (SME). The product is baby and children's clothing, and its orders were from baby shops. There were three trucks and twenty-four coordinates of customers-baby shops. The capacity of first truck was nine cubic meter, second truck was eight cubic meter, and the third truck was four cubic meter. The working hours started from 08:30 a.m to 17:30 pm and break hours
were from 12:00 to 13:00. The driver started the shipment was from warehouse and must be back to warehouse. Before running the optimoroute, there were some data must be collected: coordinates of twenty-four baby-shops, capacity of truck, volume of goods, the average time for unloading goods at the baby shops was 30 minutes, but not included waiting time: administration process such as receipt document and checking. Unloading process was in the large space.

The results from optimoroute was analyzed further by queuing simulator in order to get the effect of waiting time at the baby shop. Queuing discipline was first-in first-out (FIFO) and the server is one.

We assume that congestion can be avoided by using alternative route which is directed by Google maps and there is no restricted route.

## 3. Results and discussions

### 3.1. Results

### 3.1.1. OptimoRoute software

In figure 1, the output from optimoroute were locations, route, total time: break, travel, duration of unloading at baby shop, and total distance starting from warehouse and back to warehouse again.

Table 1 showed more detailed data, included coordinates of baby shop, order ID, stop duration and break, but unfortunately, the delivery does not always have a zero queue or waiting line at baby shop, that is why one has to consider queues by simulate various possibilities from zero to maximum customers that ever happened.

### 3.1.2. Queuing software

For the past six months observation, there were four customers per hour on the average (mean arrival rate, $\lambda$ ), and mean service rate was eight customers per hour ( $\mu$ ), the amount of server was 1 , then when the service man was busy, the other customers must wait, the queue discipline was FIFO - First In First Out. The queueing model was $\mathrm{M} / \mathrm{M} / 1$.


Fig.1. Output for normal speed
Table 1
Ouput data from optimoroute

| Order <br> ID | Vehicle | Stop <br> No. | Latitude | Longitude | Unloading duration (mnt) | Break time | $\begin{aligned} & \text { Depot } \\ & \text { to } \\ & \text { depot } \\ & (\mathrm{KM}) \end{aligned}$ | Total time (incl. stop duration and break) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ORD020 | 001 | 1 | -6.1903 | 106.5789 | 30 |  | 85 | 7 hours 52 minutes |
| ORD010 | 001 | 2 | -6.1316 | 106.7735 | 30 |  |  |  |
| ORD013 | 001 | 3 | -6.1284 | 106.8112 | 30 |  |  |  |
| ORD003 | 001 | 4 | -6.1303 | 106.8139 | 30 |  |  |  |
|  | 001 |  | -6.1303 | 106.8139 | 60 | yes |  |  |
| ORD009 | 001 | 5 | -6.1367 | 106.8198 | 60 |  |  |  |
| ORD005 | 001 | 6 | -6.1379 | 106.8231 | 30 |  |  |  |
| ORD021 | 001 | 7 | -6.1307 | 106.8162 | 30 |  |  |  |
| ORD012 | 001 | 8 | -6.1370 | 106.7953 | 30 |  |  |  |
| ORD014 | 001 | 9 | -6.1346 | 106.7718 | 30 |  |  |  |
| ORD015 | 002 | 1 | -6.1394 | 106.8733 | 45 |  | 98 | $\begin{gathered} 7 \text { hours } 56 \\ \text { minutes } \end{gathered}$ |
| ORD016 | 002 | 2 | -6.1394 | 106.8733 | 60 |  |  |  |
| ORD007 | 002 | 3 | -6.1389 | 106.8699 | 30 |  |  |  |
|  | 002 |  | -6.1389 | 106.8699 | 60 | yes |  |  |
| ORD008 | 002 | 4 | -6.1664 | 106.9046 | 45 |  |  |  |
| ORD022 | 002 | 5 | -6.1654 | 106.8742 | 30 |  |  |  |
| ORD002 | 002 | 6 | -6.1652 | 106.8754 | 30 |  |  |  |
| ORD006 | 002 | 7 | -6.1516 | 106.8751 | 30 |  |  |  |
| ORD018 | 002 | 8 | -6.1498 | 106.8213 | 30 |  |  |  |
| ORD001 | 003 | 1 | -6.1850 | 106.8158 | 30 |  | 83 | $\begin{gathered} 6 \text { hours } 36 \\ \text { minutes } \end{gathered}$ |
| ORD023 | 003 | 2 | -6.1847 | 106.8169 | 30 |  |  |  |
| ORD024 | 003 | 3 | -6.1913 | 106.8154 | 30 |  |  |  |
| ORD004 | 003 | 4 | -6.1998 | 106.8153 | 30 |  |  |  |
|  | 003 |  | -6.1998 | 106.8153 | 60 | yes |  |  |
| ORD017 | 003 | 5 | -6.2423 | 106.6543 | 30 |  |  |  |
| ORD011 | 003 | 6 | -6.2633 | 106.6622 | 30 |  |  |  |
| ORD019 | 003 | 7 | -6.2521 | 106.6199 | 30 |  |  |  |

(i) (D) Y


Fig.2. Queueing system

## Input data

| Input Parameter | The value | Explanation |
| :--- | :--- | :--- |
| Arrival Rate (1) | 4 | Help |
| Service Rate $(\mathrm{m})$ | 8 | Help |
| Experiment duration | 1000 | Help |
| Maximum queue length | 1000 | Help |


| Intro to Queuing | Some Theory | Compute Results | Run Simulation |
| :--- | :--- | :--- | :--- |

## Basic Results

| Result | Computed value | Simulated value | Explanation |
| :--- | :--- | :--- | :--- |
| Customers in system $\left(\mathrm{L}_{\mathrm{s}}\right)$ | 1 | 0.9291918280552 | Help |
| Customers in queue $\left(\mathrm{L}_{\mathrm{q}}\right)$ | 0.5 | 0.4505834791738 | Help |
| Time in system $\left(\mathrm{W}_{\mathrm{s}}\right)$ | 0.25 | 0.2368784998045 | Help |
| Time in queue $\left(\mathrm{W}_{\mathrm{q}}\right)$ | 0.125 | 0.1148377925562 | Help |
| Idle probability $\left(\mathrm{P}_{\mathrm{o}}\right)$ | 0.5 | 0.5155453618756 | Help |
| Server utilization $(\mathrm{r})$ | 0.5 | 0.4786083488814 | Help |

## Other Simulation Results

| Result | Value | Explanation |
| :--- | :--- | :--- |
| Number of arrivals | 3924 | Help |
| Minimum arrival interval | 0.0000164915354 | Help |
| Maximum arrival interval | 2.0642746794463 | Help |
| Number of services | 3923 | Help |
| Minimum service duration | 0.0000229152559 | Help |
| Maximum service duration | 0.8679524023432 | Help |
| Maximum waiting time | 1.4032821345319 | Help |
| Maximum time in system | 1.4654266814224 | Help |
| Maximum queue length | 9 | Help |

Fig 3. Results from On-Line simulator

The On-Line Simulator software provided two kinds of output, the first one was computed value and another one was simulated value. Mean arrival rate, $\lambda=4$ customers per hour and mean service rate, $\mu=8$ customers per hour are independent and exponential distributed random variable, figure 2 showed the results of computed value and simulated value.

From the above figure, there would be an additional time around 0.25 hours $=15$ minutes in systems from queue when the one delivered goods to the one baby shop. This additional queue time would produce an additional of total time in delivery. The increment of queue time was greatly related to the number of customers, in this case baby shops. If the number of baby shops increases then queue time increases. The Table 2 shows summary of additional time.

The effect of queuing time to total time

| Vehicle | Total cus- <br> tomers | Unloading <br> time <br> (hours) | Travel <br> time <br> (hours) | Total <br> time <br> (hours) | Queuing time <br> (additional <br> hours) | Total <br> time incl. <br> queue <br> (hours) | $\%$ <br> increase |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 001 | 9 | 6 | 1.87 | 7.87 | 2.25 | 10.12 | 9.12 |
| 002 | 8 | 6 | 1.93 | 7.93 | 2 | 9.93 | 8.93 |
| 003 | 7 | 4.5 | 2.10 | 6.6 | 1.75 | 8.35 | 7.35 |

Planner has to plan the route carefully, because queue time will affect maximum working hours - eight hours per day. If working hours exceed eight hours, then overtime will happen.

### 3.2. Discussion

Some activities can be predicted how long it will take such as unloading goods, waiting in the line and distance, but some factors are difficult to predict such as congestion, accidents. Congestion can be anticipated by checking Google maps, accidents can be anticipated by driving slower for crowded traffic.

## 4. Conclusions

Planning route based on distance only is not enough. Planner needs to consider queuing activities that happen at the customer's location for delivery services. By combining two methods, mTSP - OptimoRoute software and queuing theory - On Line Simulator, there was an additional time around fifteen minutes per customer's point, the more customer's point, the more time was needed. This additional time was linear to the number of customer's point.

## References

1. Dundar A.O., Ozturk, R. The effect of on-time delivery on customer satisfaction and loyalty in channel integration. Business and Management Study: An International Journal, 2020, Vol 8, Issue 3, pp.2675-2693. doi: http://dx.doi.org/10.15295/bmij.v8i3.1520.
2. Ben-Akiva M., Bierlaire M. Discrete choice methods and their applications to short term travel decisions. In: Transportation science handbook. MIT, 1999, pp.1-43.
3. Bajcetic S., Zivanovic P., Tica S., Milovanovic B. Factors influencing driving time in public transport - a multiple regression analysis. Promet - Traffic \&Transportation, 2023, Vol.35, No.1, pp. 37-54. https://doi.org/10.7307/ptt.v35i1.29.
4. Miller, M.A., Li, K. An investigation of the costs of roadway traffic congestion: a preparatory step to IVHS benefits'evaluation. California PATH research report UCB-ITS-PRR-94-15, 1994, Berkley: Institute of Transport Studies, University of California.
5. Ortuzar J.D., Willumsen L.G. Modelling transport. United Kingdom, John Wiley \& Sons, 2011.
6. Tseng Y.Y., Yue W.L., A.P. Taylor M. The role of transportation in logistics chain. Proceedings of the eastern asia society for transportation studies, 2005, vol 5, pp 1657-1662.
7. Nuriyeva F., Kizilates G.A New Heuristic Algorithm for Multiple Traveling Salesman Problem. TWMS Journal of Applied and Engineering Mathematics, 2017, Vol. 7 No.1. Department of Mathematics, Isik University.
8. Cheikhrouhou O., Khoufi I.A comprehensive survey on multiple travelling salesman problem: applications, approaches, and taxonomy. Computer Science Review, 2021. https://doi.org/10.1016/j.cosrev.2021.100369
9. Chandra A., Natalia C. Applications of multiple traveling salesman problem on zone picking. Academic Journal of Manufacturing Engineering, 2023, Vol.21, No.1, pp. 51-58.
10. Bektas T. The multiple traveling salesman problem: an overview of formulations and solution procedures. Omega, 2006, Vol.34, Issue 3, pp.209-219. https://doi.org/10.1016/j.omega.2004.10.004
11. Hillier F.S., Hillier M.S., Schmedders K., Stephens M. Introduction to management science: a modeling and case studies approach with spreadsheets. New York, McGraw Hill, 2008.
12. Sztrik J. Basic Queueing Theory. Faculty of Informatics, University of Debrecen, 2021.
13. Masson A., Paravié D., Rohvein C., Villalba L. Review of Vehicle Routing Problems Solving Software. INGECUC, 2021, Vol. 17, No.1, pp. 315-328.
DOI: http://doi.org/10.17981/ingecuc.17.1.2021.23
14. OptimoRoute, Inc. OptimoRoute. 2023. USA. www.optimoroute.com
15. Sklenar J. On-Line Simulators. 2008. Department of Statistics and Operations Research, Faculty of Science, University of Malta. www.staff.um.edu.mt/jskl1/simweb/simdown.html
